

$$\begin{aligned}
 1. \ a) \ f(x) &= -2(3x-12)^2 + 1 \\
 &= -2(3(x-4))^2 + 1 \\
 &= -2(9)(x-4)^2 + 1 \\
 &= -18(x-4)^2 + 1 \\
 &V(4, 1)
 \end{aligned}$$

$$\begin{aligned}
 b) \ f(x) &= -3|4-2x| \\
 &= -3|-2(x-2)| \\
 &= -3|-2| \cdot |x-2| \\
 &= -6|x-2| \\
 &V(2, 0)
 \end{aligned}$$

$$\begin{aligned}
 c) \ f(x) &= (6-2x)^2 \\
 &= (-2(x-3))^2 \\
 &= 4(x-3)^2 \\
 &V(3, 0)
 \end{aligned}$$

$$\begin{aligned}
 2. \ 1) \ V(-5, 7) \ P(2, 0) \\
 f(x) &= a|x+5| + 7 \\
 0 &= a|2+5| + 7 \\
 0 &= a|7| + 7 \\
 -7 &= 7a \\
 -1 &= a \\
 f(x) &= -|x+5| + 7
 \end{aligned}$$

$$\begin{aligned}
 a) \ f(0) &= -|0+5| + 7 \\
 &= -|5| + 7 \\
 &= -5 + 7 \\
 &= 2
 \end{aligned}$$

$$\begin{aligned}
 b) \ f(-3) &= -|-3+5| + 7 \\
 &= -|2| + 7 \\
 &= -2 + 7 \\
 &= 5
 \end{aligned}$$

$$\begin{aligned}
 c) \ 4 &= -|x+5| + 7 \\
 -3 &= -|x+5| \\
 3 &= |x+5|
 \end{aligned}$$

$$\begin{array}{ll}
 3 = x+5 & -3 = x+5 \\
 -2 = x & -8 = x
 \end{array}$$

$$x = \{-8, -2\}$$

$$\begin{aligned}
 d) \ -|x+5| + 7 &< 1 \\
 -|x+5| + 7 &= 1 \\
 -|x+5| &= -6 \\
 |x+5| &= 6 \\
 x+5 &= 6 & x+5 &= -6 \\
 x &= 1 & x &= -11
 \end{aligned}$$

from graph:  $f(x) < 1$   
 $x \in ]-\infty, -11[ \cup ]1, +\infty[$

2. 2)  $v(3, -2)$   $P(7, 1)$

$$f(x) = a(x-3)^2 - 2$$

$$1 = a(7-3)^2 - 2$$

$$3 = a(4)^2$$

$$3 = 16a$$

$$\frac{3}{16} = a$$

$$f(x) = \frac{3}{16}(x-3)^2 - 2$$

a)  $f(0) = \frac{3}{16}(0-3)^2 - 2$

$$= \frac{3}{16}(-3)^2 - 2$$

$$= \frac{3}{16}(9) - 2$$

$$= \frac{27}{16} - \frac{32}{16}$$

$$= \frac{-5}{16}$$

b)  $f(-3) = \frac{3}{16}(-3-3)^2 - 2$

$$= \frac{3}{16}(-6)^2 - 2$$

$$= \frac{3}{16}(36) - 2$$

$$= \frac{27}{4} - \frac{8}{4}$$

$$= \frac{19}{4}$$

c)  $4 = \frac{3}{16}(x-3)^2 - 2$

$$6 = \frac{3}{16}(x-3)^2$$

$$32 = (x-3)^2$$

$$\pm\sqrt{32} = x-3$$

$$3 + \sqrt{32} = x \quad \text{or} \quad x = 3 - \sqrt{32}$$

$$3 + 4\sqrt{2} = x \quad x = 3 - 4\sqrt{2}$$

d)  $\frac{3}{16}(x-3)^2 - 2 < 1$

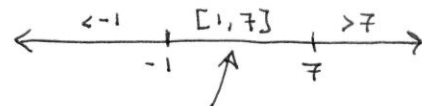
$$\frac{3}{16}(x-3)^2 - 2 = 1$$

$$\frac{3}{16}(x-3)^2 = 3$$

$$(x-3)^2 = 16$$

$$x-3 = 4 \quad x-3 = -4$$

$$x = 7 \quad x = -1$$



test  $x = 3$

$$\frac{3}{16}(3-3)^2 - 2 < 1$$

$$0 - 2 < 1$$

$$-2 < 1 \quad \text{True}$$

$$\therefore f(x) < 1$$

$$x \in ]-1, 7[$$

$$5. \quad P(x) = -|100 - 2x| + 70$$

$$a) \quad P = 0$$

$$0 = -|100 - 2x| + 70$$

$$-70 = -|100 - 2x|$$

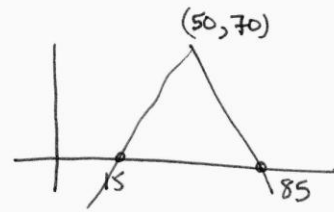
$$70 = |100 - 2x|$$

$$100 - 2x = 70 \quad \text{OR} \quad 100 - 2x = -70$$

$$30 = 2x \quad \text{OR} \quad 170 = 2x$$

$$15 = x \quad \text{OR} \quad 85 = x$$

$[15, 85]$  subscriptions



$$f(x) = -|-2(x-50)| + 70$$

$$f(x) = -2|x-50| + 70$$

$$b) \quad x = 40 \quad f(40) = -|100 - 2(40)| + 70$$

$$= -|100 - 80| + 70$$

$$= -|20| + 70$$

$$= -20 + 70$$

$$= 50$$

The profit is \$ 50

$$c) \quad f(x) \geq 50$$

$$50 = -|100 - 2x| + 70$$

$$-20 = -|100 - 2x|$$

$$20 = |100 - 2x|$$

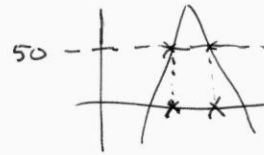
$$20 = 100 - 2x \quad \text{OR} \quad -20 = 100 - 2x$$

$$2x = 80$$

$$x = 40$$

$$2x = 120$$

$$x = 60$$



$[40, 60]$  subscriptions

$$6. P(n) = -12n - 160 + 50$$

$$P(n) = -12(n-80) + 50$$

$$P(n) = -2|n-80| + 50$$

$$a) v(80, 50)$$

$$(0, -110)$$

$$0 = -2|n-80| + 50$$

$$-50 = -2|n-80|$$

$$25 = |n-80|$$

$$n-80 = 25$$

$$n = 105$$

$$n-80 = -25$$

$$n = 55$$

$$b) x = 100$$

$$f(100) = -2|100-80| + 50$$

$$= -2|20| + 50$$

$$= -40 + 50$$

$$= 10$$

\$ 10 profit

$$c) 40 = -2|x-80| + 50$$

$$-10 = -2|x-80|$$

$$5 = |x-80|$$

$$x-80 = 5 \quad \text{or} \quad x-80 = -5$$

$$x = 85$$

$$x = 75$$

75 or 85 magnets

$$d) f(60) = -2|60-80| + 50$$

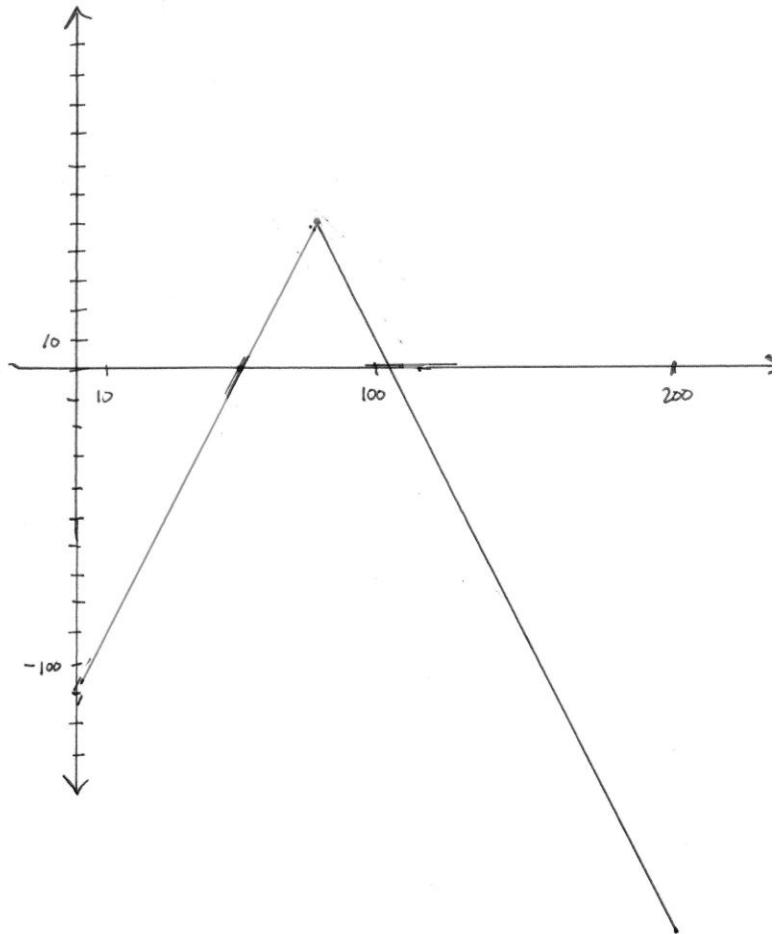
$$= -2|-20| + 50$$

$$= -2(20) + 50$$

$$= -40 + 50$$

$$= 10$$

\$ 10 profit



7.  $f(x) = -|x-4| + 3$

Vertex:  $(4, 3)$

Axis of symmetry:  $x=4$

$$2 = -|x-4| + 3$$

$$-1 = -|x-4|$$

$$1 = |x-4|$$

$$1 = x-4 \text{ or } -1 = x-4$$

$$5 = x \quad 3 = x$$



$$0 = -|x-4| + 3$$

$$-3 = -|x-4|$$

$$3 = |x-4|$$

$$3 = x-4 \text{ or } -3 = x-4$$

$$7 = x \quad 1 = x$$

$$f(x) \leq 2: ]-\infty, 3] \cup [5, +\infty[$$

$$\text{Zeros: } x = \{1, 7\}$$

$$g(x) = |2x+1| - 3$$

Vertex:  $(-1/2, -3)$

$$g(x) = |2(x+1/2)| - 3$$

$$g(x) = 2|x+1/2| - 3$$

Axis of Symmetry:  $x = -1/2$

$$g(x) \leq 2: [-3, 2]$$

$$2 = |2x+1| - 3$$

$$5 = |2x+1|$$

$$\text{Zeros: } \{-2, 1\}$$

$$5 = 2x+1 \quad -5 = 2x+1$$

$$4 = 2x \quad -6 = 2x$$

$$2 = x \quad -3 = x$$



$$0 = |2x+1| - 3$$

$$3 = |2x+1|$$

$$2x+1 = 3$$

$$2x = 2$$

$$x = 1$$

$$2x+1 = -3$$

$$2x = -4$$

$$x = -2$$

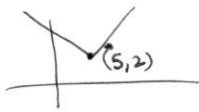
$$h(x) = 3|x-5| + 2$$

Vertex:  $(5, 2)$

Axis of symmetry:  $x = 5$

$h(x) \leq 2$ :  $x = 5$  (vertex)

Zeros: none



$$j(x) = -4|2x-3|$$

Vertex:  $(\frac{3}{2}, 0)$

$$j(x) = -4|2(x-\frac{3}{2})|$$

Axis of symmetry:  $x = \frac{3}{2}$

$$j(x) = -8|x-\frac{3}{2}|$$

$j(x) \leq 2$ :  $\mathbb{R}$  (whole function is  $\leq 2$ )

Zeros:  $x = \frac{3}{2}$  (vertex)

