

## Function Parameters

- Every "family" has a **basic** or **parent** function - the simplest form of that function.  
 Eg:  $y = x$        $y = x^2$        $y = \sqrt{x}$        $y = \frac{1}{x}$
- We can transform a function by changing certain values called **parameters**.
- We consider four parameters:  **$a$ ,  $b$ ,  $h$  &  $k$** .

In a basic function,

$$a = 1$$

$$b = 1$$

$$h = 0$$

$$k = 0$$

Parameter  $h$

Summary:

Parameter  $h$  causes a translation or shift of the function to the left or to the right  $h$  units.

$h > 0$  shift to the right

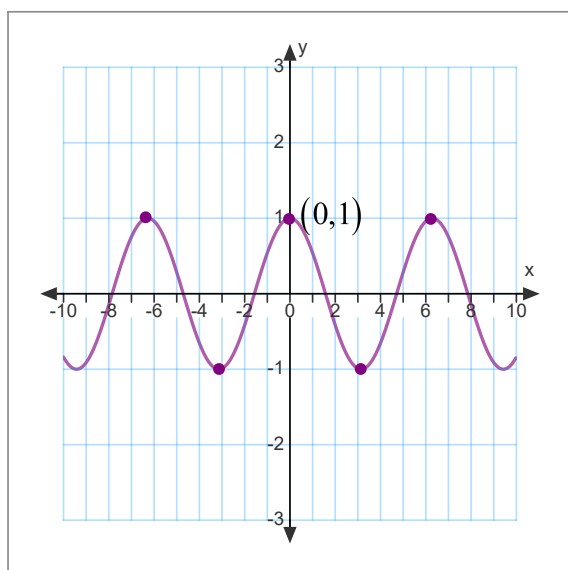
$h < 0$  shift to the left

The rule or equation is written  $(x - h)$ .

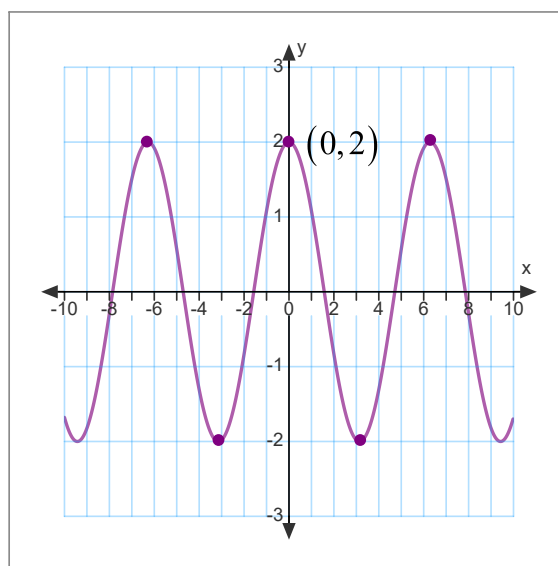
Parameter  $a$

In a basic function  $a = 1$ .

$$y = \cos x$$



$$y = 2 \cos x \quad (a = 2)$$



Parameter  $a$  (basic function  $a = 1$ .)

Parameter  $a$  affects a function's relationship with the  $x$ -axis.

$|a| > 1$  the function moves away from the  $x$ -axis. (vertical stretch)

$|a| < 1$  the function moves towards the  $x$ -axis. (vertical compression)

$a < 0$  the function is reflected about the  $x$ -axis.

Parameter  $b$  (basic function:  $b = 1$ )

Parameter  $b$  affects a function's relationship with the  $y$ -axis.

$|b| > 1$  the function moves towards the  $y$ -axis  
(horizontal compression).

$|b| < 1$  the function moves away from the  $y$ -axis  
(horizontal stretch).

$b < 0$  the function is reflected about the  $y$ -axis.

Example of a function

Basic

$$y = \sqrt{x}$$

$$a = 1$$

$$b = 1$$

$$h = 0$$

$$k = 0$$

Transformed (with parameters)

$$y = 2\sqrt{-4(x-6)} - 8$$

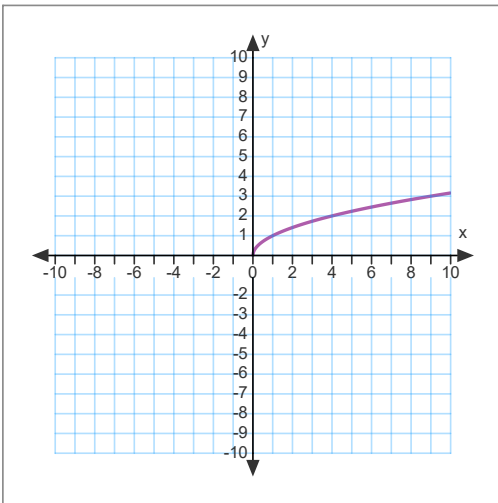
$$a = 2$$

$$b = -4$$

$$h = 6$$

$$k = -8$$

$$y = \sqrt{x}$$



$$y = 2\sqrt{-4(x-6)} - 8$$

