

Simplify:

$$a) \frac{\overset{\text{D.O.S}}{a^2 - 1}}{a + 1} = \frac{(a - 1)\cancel{(a + 1)}}{\cancel{(a + 1)}}$$

$$\left. \begin{array}{l} a + 1 = 0 \\ a = -1 \end{array} \right\} a \neq -1$$

$$a \neq -1, a \neq -1$$

$$b) \frac{2x + 10}{1x^2 + 7x + 10}$$

$\frac{m \times n}{m + n} \quad 2, 5$

$$\frac{2\cancel{(x + 5)}}{\cancel{(x + 5)}(x + 2)}$$

$$\left. \begin{array}{l} (x + 5)(x + 2) = 0 \\ x + 5 = 0 \text{ or } x + 2 = 0 \\ x = -5 \quad x = -2 \end{array} \right\} x \neq \{-5, -2\}$$

$$\frac{2}{x + 2}, x \neq \{-5, -2\}$$

$$c) \frac{v^2 - 7v - 30}{v^2 - 5v - 24}$$

$$d) \frac{6m^3 + 42m^2}{2m^2 + 26m + 84}$$

$$\frac{6m^2(m+7)}{2(m^2+13m+42)}$$

$$\left. \begin{array}{l} m \times n = 42 \\ m+n = 13 \end{array} \right\} \begin{array}{l} 6,7 \\ 7,6 \end{array}$$

$$\frac{6m^2(m+7)}{2(m+7)(m+6)}$$

$$\left. \begin{array}{l} m+6=0 \\ m=-6 \end{array} \right\} m \neq \{-7, -6\}$$

$$\left. \begin{array}{l} m+7=0 \\ m=-7 \end{array} \right\} \{-7, -6\}$$

$$\frac{3m^2}{m+6}, m \neq \{-7, -6\}$$

Rational Expressions and Arithmetic

To add, subtract, multiply & divide rational expressions, we are going to use the rules of arithmetic for fractions as well as our methods for factoring and simplifying.

1. Multiplication

Example: $\left(\frac{3a-3b}{a}\right)\left(\frac{a^2}{a-b}\right)$

* factor each polynomial, if possible

$$\left(\frac{3(a-b)}{a}\right)\left(\frac{a^2}{a-b}\right) \quad \left. \begin{array}{l} a=0 \\ a-b=0 \end{array} \right\} a \neq \{0, b\}$$

* state the restrictions, then multiply the expressions (canceling any common factors on top and bottom).