## Objective Function

A system of linear inequalities has many solutions.
Depending on the situation, some of these solutions (usually one) are better than the others and will be called the optimal solution. What determines this optimal solution is the objective function or objective rule.

Example:
A farmer grows cherries \& raspberries on a piece of land that is at most $16 h a$ in area. Each hectare of cherries requires 5 days of work and each hectare of raspberries, 3 days of work. The farmer has no more than 60 days available. He decides that the space for raspberries will be at most 3 times the amount of space for cherries. Each hectare of cherries and rasperries produces revenues of $\$ 3000$ and $\$ 5000$ respectively. What is the maximum revenue the farmer can earn?


The farmer's objective is to make the maximum revenue possible given the constraints.
The objective rule for this farmer is $R=3000 x+5000 y$



| Points | Rewe |
| :---: | :---: |
| $(0,0)$ | \$ 0 |
| $(4,10)$ | 62000 |
| $v(4,12)$ | 72000 |
| $\checkmark(6,10)$ | 68000 |
| $\checkmark(12,0)$ | 3600 |
|  | 000 |

The optimal solutions (maximum or minimum) occur on the boundary of the solution set and usually occur only at the vertices.

Solving Optimisation Problems
i. Define the variables.
2. List the constraints.
3. Write the objective function.
4. Graph the polygon of constraints.
5. Determine the coordinates of the vertices of the polygon.
6. Identify the optimal solution - the maximum or minimum that solve the problem.

