

Sum and Difference of Two Angles

There are formulae that allow us to determine the sine, cosine and tangent of the sum or difference of two angles.

	Sum	Difference
Sine	$\sin(a + b) = \sin a \cos b + \sin b \cos a$	$\sin(a - b) = \sin a \cos b - \sin b \cos a$
Cosine	$\cos(a + b) = \cos a \cos b - \sin a \sin b$	$\cos(a - b) = \cos a \cos b + \sin a \sin b$
Tangent	$\tan(a + b) = \frac{\tan a + \tan b}{1 - \tan a \tan b}$	$\tan(a - b) = \frac{\tan a - \tan b}{1 + \tan a \tan b}$

We can use these rules to determine the exact values of some angles not found on the trig circle.

Examples: Determine the exact values of ...

1. $\sin \frac{23\pi}{12}$

2. $\cos 15^\circ$

$$3. \quad \tan\left(-\frac{\pi}{12}\right)$$

4. $\sec 165^\circ$

We can also use these rules to prove some statements.

Examples: *Show that ...*

1. $\sin(9\pi - x) = \sin x$

$$2. \tan(x - 4\pi) = \tan x$$

Can you find an expression that corresponds to ...

1. $\sin(2\theta)$

2. $\cos 2\theta$

These expressions are also rules and are known as the double angle formulas.

Given $P(\theta) = \left(\frac{8}{17}, -\frac{15}{17}\right)$, find the coordinates of $P(2\theta)$.

Knowing that $\sin a = -\frac{15}{17}$ and $\sin b = \frac{12}{13}$, and that $\frac{3\pi}{2} \leq a \leq 2\pi$ and $\frac{\pi}{2} \leq b \leq \pi$ calculate...

$$\sin(a + b)$$

$$\cos(a - b)$$

Work Book: Page 254 & 255

Questions 1,4 & 6