

1

What is the numerical value of the following logarithmic expressions?

a)  $\log_2 \sqrt{8} + \log_3 \frac{1}{3} + 6^{\log_6 1}$

b)  $\log_{\frac{1}{3}} 27 + 2\log_2 4^2 + \log_5 \sqrt{5} - 2\log_5 1$

2

Solve the following equations:

a)  $\log(2x - 5) + \log(x - 1) = 2\log 2 + \log 5$

b)  $\log_2(x + 3) + \log_2(2x + 4) - \log_{11} 121 = 0$

c)  $3\log_a 2 + \log_a(x - 2) = \log_a 12(x + 3) - \log_a 3$

d)  $\log_3(x + 4) = \log_7 7 - \log_3(x + 2)$

e)  $\log(x + 3) + \log(2x - 7) = \log(2x - 1)$

f)  $2^x = 3^{2x-1}$

3

Given  $\log_n u = 7$  and  $\log_n w = -9$ , what is the value the following expression  $\log_n \left( \frac{n^2 w^4}{u^5} \right)$ ?

4

Use the properties of logarithms to express  $\log_2 \left( \frac{\sqrt{x}(x-5)}{x^3} \right)$  as a sum, a difference or a product of logarithms.

5

Given the following equation:  $2\log_a 8 + \log_a \left( \frac{1}{a} \right)^5 = 19$ . What is the numerical value of base a?

6

The increasing logarithmic function f has domain  $]5, +\infty[$ . The graph of this function passes through the point (9, 10). Which of the following functions could represent function f?

A)  $f(x) = 3\log_2(x - 5) + 4$

C)  $f(x) = 5\log_{\frac{1}{2}}(x - 1) + 5$

B)  $f(x) = \log_4(x - 5) + 8$

D)  $f(x) = 15\log_{14}(x + 5) - 5$

7

If  $f(x) = 3^{(x-9)}$  and  $g(x) = \log_9 x$ , what is  $(g \circ f)(x)$ ?

8

Given  $f(x) = 2(5^{x+1})$ , then which of the following represents  $f^{-1}(x)$ ?

A)  $f^{-1}(x) = \log_5 \left( \frac{x}{2} - 1 \right)$

C)  $f^{-1}(x) = \log_{10} \left( \frac{x}{2} - 1 \right)$

B)  $f^{-1}(x) = \log_5 \left( \frac{x}{2} \right) - 1$

D)  $f^{-1}(x) = \log_{10}(x - 1)$

9

A microbiologist is studying two bacteria populations.

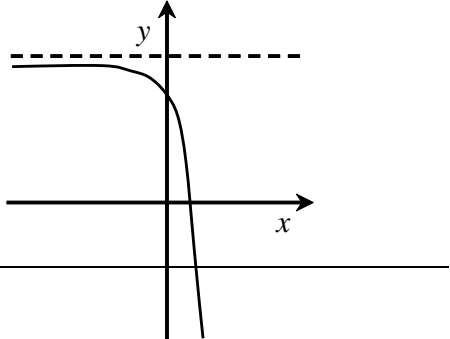
Last Monday, the 1<sup>st</sup> population numbered 2000 and the 2<sup>nd</sup> numbered 2 048 000.

He noted that the 1<sup>st</sup> population doubled every day while the 2<sup>nd</sup> population was reduced by half each day. After how many days would the two populations of bacteria be equal in number?

10

The rule of a function  $g$  is  $g(x) = a(c)^x + k$ . The equation of its asymptote is  $y = 8$ . This function is represented by the table of values and the graph given below. **What is the rule of function  $g$ ?**

$x$	$y$
0	6
1	2
2	-10



11

Reproduction of a certain type of insect is the focus of a laboratory experiment. There were 25 insects at the beginning of the experiment. It was noted that the number of insects increases by 3% every 7 days. **After how many days will there be 20 425 insects?**

12

The number of people living in Kilwat, Germany, varies according to the rule of an exponential function. On January 1<sup>st</sup> 1975, the city's population was 130 000. On January 1<sup>st</sup> 1985, it was 260 000. **What was the population of this German city on January 1<sup>st</sup> 2010, given that the growth rate remained constant?**

13

Three years ago Greg invested \$1000 at a fixed interest rate compounded every 6 months. His investment is currently valued at \$1400. Given  $C_n = C_0 \left(1 + \frac{t}{k}\right)^{nk}$  where  $C_n$  is the capital after  $n$  years,  $C_0$  is the capital invested,  $t$  is the annual interest rate,  $k$  is the number of times per year that interest is paid and  $n$  is the number of years, **what is the annual rate of interest?**

14

In a laboratory, the reproduction of a particular species of insect is studied. At the beginning of the experiment, there are 25 insects. The number of insects increases by 30% every 7 days. **After how many weeks will there be 20 425 insects?**

15

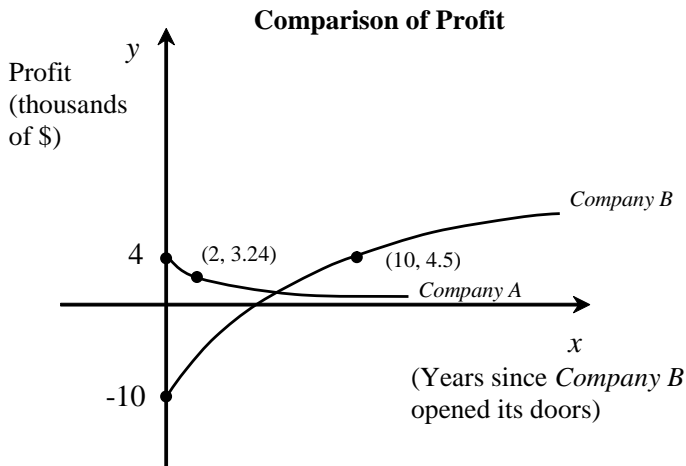
When Jennifer bought a new car in 2005, she paid \$17 500. In 2008 the value of her car had fallen to \$10 000. She decided that she would sell her car when the value fell below \$5000. Assuming the decline in the price of a car is modelled by an exponential function, **how old will Jennifer's car be when its value falls below \$5000?**

16

A virus appeared in South America in the middle of the last decade. Scientists knew that the number of people infected with this virus would increase according to a specific exponential function. At the beginning of 1996, authorities found 110 infected people. Five years later, the number had grown to 835. Wide-scale inoculation began once 2000 people had been infected with the virus. **In what year did these inoculations begin?**

17

*Company A* has seen a decrease in profit since its competitor, *Company B*, opened its doors. The decrease can be estimated using an exponential function in the form of  $g(x) = ac^x$ . The profit of *Company B* can be estimated according to an exponential function in the form of  $f(x) = ac^x + 15$ . Based on these estimates, **how much more profit would *Company B* make than *Company A*, 11 years after it opened its doors?**



18

When rabbits were first brought to Australia, they had no natural enemies. From January 1865 to January 1867, the rabbit population increased exponentially from 60 000 members to 2 400 000 members. According to this exponential model, **in which year were the first pair of rabbits brought to Australia?**